

Height of a pop-up: A baseball is hit straight up from a height of 4 feet with an initial velocity of 70 ft/sec.

- Write an equation that models the height of the ball as a function of time.
- Use parametric mode to simulate the pop-up.
- Use parametric mode to graph height against time. (Let $x(t) = t$)
- How high is the ball after 3 seconds?
- What is the maximum height of the ball? How many seconds does it take to reach its maximum height?

Hitting a baseball: Kevin hits a baseball at 3 feet above the ground with an initial speed of 150ft/sec at angle of 18 degrees with the horizontal.

* Will the ball clear a 20 feet wall that is 400 feet away?

$$x = 150t \cos 18$$

$$y = 150t \sin 18 - 16t^2 + 3$$

$$\frac{400 = 150t \cos 18}{150 \cos 18} \quad \frac{400}{150 \cos 18}$$

$$2.803 = t \text{ seconds}$$

After 2.803 sec the ball is 7.178ft High

The ball will not clear a 20ft wall

The men's horseshoe pitching court has metal stakes **40 feet apart**. The stakes stand **18 inches** out of the ground.

a. Alan pitches a horseshoe at **45 feet per second**, at a **14° angle** to the ground. He releases the horseshoe at about **3 feet above** the ground and **2 feet in front** of the stake at one end. **Write parametric equations** modeling a typical throw.

$$x = 45t \cos 14^\circ + 2 \quad y = 45t \sin 14^\circ - 16t^2 + 3$$

b. How long is the thrown horseshoe in the air? (*Hits the ground*)

$$0 = 45t \sin 14^\circ - 16t^2 + 3$$

$$y = 0$$

$$t = .890 \text{ sec}$$

c. How close to 40ft is the horizontal component when the horseshoe hits the ground?

$$t = .89 \text{ sec hit ground}$$

$$\text{plug } t \text{ into } x = 45t \cos 14^\circ + 2$$

$$x = 40.89 \text{ ft}$$

$$.89 \text{ ft away}$$

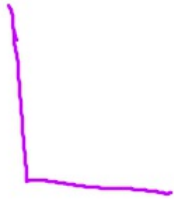
$$.89 \times 12 \text{ in} = 10.68 \text{ inches away}$$

$$x = vt \cos 20^\circ + 1.5$$

$$\begin{array}{r} 40 = vt \cos 20^\circ + 1.5 \\ -1.5 \qquad \qquad \qquad -1.5 \end{array}$$

$$\frac{38.5}{v \cos 20^\circ} = \frac{vt \cos 20^\circ}{v \cos 20^\circ}$$

$$\boxed{\frac{38.5}{v \cos 20^\circ} = t}$$



$$\boxed{y = vt \sin 20^\circ - 16t^2 + 2}$$

$$18 \text{ inch} = 1.5 \text{ ft}$$

y is between $\boxed{0}$ and 1.5 ft

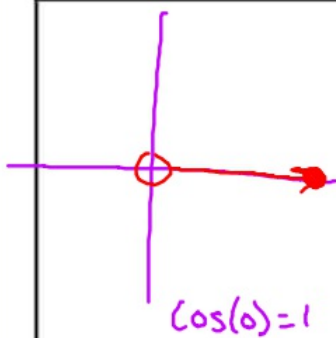
$$0 = v \left(\frac{38.5}{v \cos 20^\circ} \right) \sin 20^\circ - 16 \left(\frac{38.5}{v \cos 20^\circ} \right)^2 + 2$$

$$\boxed{0 = \left(\frac{38.5}{\cos 20^\circ} \right) \sin 20^\circ - 16 \left(\frac{38.5}{v \cos 20^\circ} \right)^2 + 2}$$

$$0 = 38.5 \tan 20^\circ -$$

$$\boxed{v = 40.95 \text{ ft/sec}}$$

Between 40.95 and 43 ft/sec



Joan Embury has spent much of her life researching the behavior of gorillas. Before examining injured gorillas, she must use a tranquilizer dart gun to sedate them. Her tranquilizer dart gun shoots darts at about 650 feet per second. Suppose Joan shot a dart (aimed horizontally at 5 ft above the ground) at a large injured gorilla 400 ft away.

a. Will the dart reach the gorilla?

$$x = 650t \cos(0)$$

$$x = 650t$$

$$400 = 650t$$

$$y = 650t \sin(0) - 16t^2 + 5$$

$$y = -16t^2 + 5 \quad y = -1.059$$

b. At what angle should Joan's aim be adjusted so that she can hit the gorilla at a point somewhere between 2 and 5 ft above the ground?

$$x = 650t \cos \theta$$

$$y = 650t \sin \theta - 16t^2 + 5$$

$$\frac{400 = 650t \cos \theta}{650 \cos \theta \quad 650 \cos \theta}$$

$$2 = \frac{650/400}{650 \cos \theta} \sin \theta - 16 \left(\frac{400}{650 \cos \theta} \right)^2 + 5$$

$$\frac{400}{650 \cos \theta} = t$$

$$2 = 400 \tan \theta - 16 \left(\frac{400}{650 \cos \theta} \right)^2 + 5$$

$$\theta = .43^\circ \text{ and } \theta = .86^\circ$$

c. How much leeway does Joan have in choosing the angle at which to shoot?