

$2n+1 \rightarrow$ Odd #'s
 $2n \rightarrow$ Even #'s

Notes

! Factorial

$0! = 1$

$1! = 1$

$2! = 2 \cdot 1 = 2$

$3! = 3 \cdot 2 \cdot 1 = 6$

$4! = 4 \cdot 3 \cdot 2 \cdot 1 = 24$

$5! = 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 = 120$

$6! = 720$

Find the first 5 terms of the sequence

62) $a_n = \frac{1}{(n+1)!}$

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$\frac{1}{2}, \frac{1}{6}, \frac{1}{24}, \frac{1}{120}, \frac{1}{720}$
 $n=1 \quad n=2 \quad n=3$

Simplify

70) $\frac{(10! \cdot 3!)}{(4! \cdot 6!)}$

Simplify

$$\frac{(10! \cdot 3!)}{(4! \cdot 6!)} = \frac{10 \cdot 9 \cdot 8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1 \cdot 3 \cdot 2 \cdot 1}{4 \cdot 3 \cdot 2 \cdot 1 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}$$

$$= \frac{10 \cdot 9 \cdot \cancel{8} \cdot 7}{4} = 1260$$

68. $a_n = \frac{(-1)^{2n+1}}{(2n+1)!}$

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$n=1 \quad n=2$

$\frac{-1}{6}, \frac{-1}{120}, \frac{-1}{5040}, \frac{-1}{362880}, \frac{-1}{11!}$

$\frac{(-1)^3}{3!}, \frac{(-1)^5}{5!}$

Simplify

$$72) \frac{(n+2)!}{n!}$$

$$72) \frac{(n+2)!}{n!} = \frac{(n+2)(n+1)(\cancel{n})(\cancel{n-1})(\cancel{n-2}) \dots}{\cancel{n}(\cancel{n-1})(\cancel{n-2}) \dots}$$
$$= (n+2)(n+1)$$

$$74) \frac{(2n+2)!}{(2n)!}$$

$$\frac{(2n+2)!}{(2n)!} = \frac{(2n+2)(2n+1)(\cancel{2n})(\cancel{2n-1}) \dots}{(\cancel{2n})(\cancel{2n-1})(\cancel{2n-2}) \dots}$$

$$\frac{(2n)!}{(2n+2)!} = \frac{1}{(2n+2)(2n+1)}$$

$$\frac{(3n+4)!}{(3n)!} = (3n+4)(3n+3)(3n+2)(3n+1)(\cancel{3n}) \dots$$

NOTES

Write the expression for the nth term.

40) 3, 7, 11, 15, 19, ...

$$a_n = a_1 + d(n-1)$$

$$a_n = 3 + 4(n-1)$$

$$= 3 + 4n - 4$$

$$a_n = 4n - 1$$

$2n+1 \rightarrow$ odds
 $2n-1 \rightarrow$

44) $\frac{2}{1}, \frac{3}{3}, \frac{4}{5}, \frac{5}{7}, \frac{6}{9}, \dots$

$$a_n = \frac{2 + 1(n-1)}{1 + 2(n-1)}$$

$$a_n = \frac{2 + n - 1}{1 + 2n - 2} = \frac{n+1}{2n-1}$$

48) $1 + \frac{1}{2}, 1 + \frac{3}{4}, 1 + \frac{7}{8}, 1 + \frac{15}{16}, 1 + \frac{31}{32}, \dots$

$\begin{matrix} +2 & +4 & +8 & +16 \\ \wedge & \wedge & \wedge & \wedge \\ 1 & 1 & 1 & 1 \\ \wedge & \wedge & \wedge & \wedge \\ +2 & +4 & +8 & +16 \end{matrix}$

$$a_n = 1 + \frac{2^n - 1}{2(2^{n-1})}$$

$$= 1 + \frac{2(2^{n-1}) - 1}{2(2^{n-1})}$$

$$a_n = \frac{2^{n-1}}{(n-1)!}$$

0, 3, 8, 15, 24

$\begin{matrix} \vee & \vee & \vee & \vee \\ +3 & +5 & +7 & +9 \end{matrix}$

42) $\frac{1}{1}, \frac{1}{4}, \frac{1}{9}, \frac{1}{16}, \frac{1}{25}, \dots$

$$a_n = \frac{1}{n^2}$$

1, 4, 9, 16, 25

$\begin{matrix} \vee & \vee & \vee & \vee \\ +3 & +5 & +7 & +9 \end{matrix}$

46) $\frac{1}{3}, \frac{-2}{9}, \frac{4}{27}, \frac{-8}{81}, \dots$

$$a_n = a_1 (r)^{n-1} \quad a_n = \frac{1}{3} \left(-\frac{2}{3}\right)^{n-1}$$

$$a_n = \frac{1(-2)^{n-1}}{3(3)^{n-1}}$$

50) $1, 2, \frac{2^2}{2}, \frac{2^3}{6}, \frac{2^4}{24}, \frac{2^5}{120}, \dots$

$n=1$ \leftarrow $n=2$ $n=3$ $n=4$ $n=5$ $n=6$

$\frac{2^0}{0!}, \frac{2^1}{1!}, \frac{2^2}{2!}, \frac{2^3}{3!}, \frac{2^4}{4!}, \frac{2^5}{5!}$

Find the Sum