

$$\text{Sum} = \frac{\text{1st term}}{1-r}$$

Find the interval of Convergence and the function that represents the series

$$24) \sum_{n=0}^{\infty} \frac{(x+1)^{2n}}{9^n} =$$

$$r = \frac{(x+1)^2}{9}$$

$$S = \frac{1}{1 - \frac{(x+1)^2}{9}}$$

$$-1 < \frac{(x+1)^2}{9} < 1$$

$$-9 < (x+1)^2 < 9$$

$$\begin{array}{ccc} -3 & < & x+1 & < & 3 \\ -1 & & -1 & & -1 \end{array}$$

$$\hline -4 < x < 2$$

$$28) \sum_{n=0}^{\infty} \left(\frac{\sin x}{2} \right)^n =$$

What you'll Learn About
Testing Endpoints for Convergence

Find the interval
 of convergence

24) $\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n (x-1)^n =$

$$r = \frac{2}{3}(x-1)$$

$$-1 < \frac{2}{3}(x-1) < 1$$

$$-\frac{3}{2} < x-1 < \frac{3}{2}$$

$$-\frac{1}{2} < x < \frac{5}{2}$$

$x = -\frac{1}{2}$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(-\frac{3}{2}\right)^n = \sum_{n=0}^{\infty} (-1)^n$$

$\lim_{n \rightarrow \infty} |(-1)^n| \neq 0$ diverges

$x = \frac{5}{2}$

$$\sum_{n=0}^{\infty} \left(\frac{2}{3}\right)^n \left(\frac{3}{2}\right)^n = \sum_{n=0}^{\infty} (1)^n$$

$\lim_{n \rightarrow \infty} (1)^n \neq 0$ diverges

$$-1 < 3x-1 < 1$$

$$0 < 3x < 2$$

$$0 < x < \frac{2}{3}$$

Absolute
 convergence

5) $\sum_{n=0}^{\infty} \frac{(-1)^n (3x-1)^n}{n^2} =$

$$\lim_{n \rightarrow \infty} \left| \frac{(-1)^{n+1} (3x-1)^{n+1}}{(n+1)^2} \cdot \frac{n^2}{(-1)^n (3x-1)^n} \right| = \left| \frac{(3x-1)^{n+1} n^2}{(n+1)^2} \right| = |3x-1| < 1$$

$x=0$

$$\sum_{n=0}^{\infty} \frac{(-1)^n (-1)^n}{n^2} = \sum_{n=0}^{\infty} \frac{(1)^n}{n^2} = \sum_{n=0}^{\infty} \frac{1}{n^2} \quad p=2 > 1 \text{ converges}$$

$x = \frac{2}{3}$

~~conditional convergence~~ b/c the series alternate
 and the terms decrease in absolute value
 Absolute convergence $\rightarrow \sum_{n=0}^{\infty} \frac{1}{n^2} \quad p=2 > 1$

$-1 < x < 1 \rightarrow \text{Interval}$

$$\lim_{n \rightarrow \infty} \left| \frac{(-1)^n}{\sqrt{n}} \right| = 0 \quad \left| \frac{(-1)^{n+1}}{\sqrt{n+1}} \right| < \left| \frac{(-1)^n}{\sqrt{n}} \right|$$

$-1 < x < 1$

$x = -1$
Conditional convergence

Absolute Converges
 $-1 < x < 1$

Conditional convergence
 $x = -1$

9) $\sum_{n=0}^{\infty} \frac{x^n}{\sqrt{n}} =$

$$\lim_{n \rightarrow \infty} \left| \frac{x^{n+1}}{\sqrt{n+1}} \cdot \frac{\sqrt{n}}{x^n} \right| = \left| \frac{x \sqrt{n}}{\sqrt{n+1}} \right| = |x| < 1$$

$x = -1$
 $\sum_{n=0}^{\infty} \frac{(-1)^n}{\sqrt{n}}$

Conditional convergence b/c the series alternates and the absolute value of the terms approach 0.

$x = 1$
 $\sum_{n=0}^{\infty} \frac{1}{\sqrt{n}} \rightarrow p = \frac{1}{2} < 1$ diverges

Absolute? NO
 $\sum \frac{1}{\sqrt{n}} \quad p = \frac{1}{2} < 1$

13) $\sum_{n=0}^{\infty} \frac{n!}{2^n} x^{2n} =$

1) $\sum_{n=0}^{\infty} \frac{(-x)^n}{n!} =$

2015 AP Calculus BC Free Response

6. The Maclaurin Series for a function f is given by

$$\sum_{n=1}^{\infty} \frac{(-3)^{n-1}}{n} x^n = x - \frac{3}{2}x^2 + 3x^3 - \dots + \frac{(-3)^{n-1}}{n} x^n + \dots$$

and converges to $f(x)$ for $|x| < R$, where R is the radius of convergence of the Maclaurin series.

a) Use the Ratio Test to find R .

20. What are all values of x for which the series $\sum_{n=1}^{\infty} \frac{(x-2)^n}{n3^n}$ converges?

(A) $-3 \leq x \leq 3$ (B) $-3 < x < 3$ (C) $-1 < x \leq 5$ (D) $-1 \leq x \leq 5$ (E) $-1 \leq x < 5$