

Consider the differential equation $\frac{dy}{dx} = 1 - y$. Let $y = f(x)$ be the particular solution to this differential equation with the initial condition $f(1) = 0$. For this particular solution, $f(x) < 1$ for all values of x .

- a) Use Euler's Method, starting at $x = 1$ with two steps of equal size, to approximate $f(0)$. Show the work that leads to your answer.

Consider the differential equation $\frac{dy}{dx} = 3x + 2y + 1$.

- b) Let $y = f(x)$ be a particular solution to the differential equation with the initial condition $f(0) = -2$. Use Euler's method, starting at $x = 0$ with a step size of .5, to approximate $f(1)$. Show the work that leads to your answer.

Consider the differential equation $\frac{dy}{dx} = 5x^2 - \frac{6}{y-2}$ for $y \neq 2$. Let $y = f(x)$ be the particular solution to this differential equation with the initial condition $f(-1) = -4$.

- d) Use Euler's Method, starting at $x = -1$ with two steps of equal size, to approximate $f(0)$. Show the work that leads to your answer.

Let f be the function satisfying $f'(x) = -3xf(x)$, for all real numbers x , with $f(1) = 4$ and

$$\lim_{x \rightarrow \infty} f(x) = 0.$$

- a) Use Euler's Method, starting at $x = 1$ with a step size of .5, to approximate $f(2)$.

Let f be the function whose graph goes through the point $(3, 6)$ and whose derivative is given by

$$f'(x) = \frac{1 + e^x}{x^2}$$

b) Use Euler's Method, starting at $x = 3$ with a step size of $.05$, to approximate $f(3.1)$. Use f'' to explain why this approximation is less $f(3.1)$.

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Consider the differential equation $\frac{dy}{dx} = y^2(2x + 2)$. Let $y = f(x)$ be the particular solution to the differential equation with initial condition $f(0) = -1$.

a) Use Euler's method, starting at $x = 0$ with two steps of equal size, to approximate $f(.5)$.

7. Given that $y(1) = -3$ and $\frac{dy}{dx} = 2x + y$, what is the approximation for $y(2)$ if Euler's Method is used with step size of $.5$, starting at $x = 1$.

- A) -5 B) -4.25 C) -4 D) -3.75 E) -3.5

Let $y = f(x)$ be the solution to the differential equation $\frac{dy}{dx} = x - y$ with initial condition $f(1) = 3$.

What is the approximation for $f(2)$ obtained by using Euler's Method with two steps of equal length starting at $x = 1$?

- A) $\frac{-5}{4}$ B) 1 C) $\frac{7}{4}$ D) 2 E) $\frac{21}{4}$

7. Let $y = f(x)$ be the solution to the differential equation $\frac{dy}{dx} = x - y - 1$ with the initial condition $f(1) = -2$. What is the approximation for $f(1.4)$ if Euler's Method is used, starting at $x = 1$ with two steps of equal size.

- A) -2 B) -1.24 C) -1.2 D) -0.64 E) 0.2