

What you will learn about:  
Adding and Subtracting Square Roots

### Adding and Subtracting Like Square Roots

$$2\sqrt{2} - 7\sqrt{2}$$

$$-5\sqrt{2}$$

$$3\sqrt{y} + 4\sqrt{y}$$

$$7\sqrt{y}$$

$$5\sqrt{13} + 4\sqrt{13} + 2\sqrt{13}$$

$$11\sqrt{13}$$

$$1\sqrt{7x} - 7\sqrt{7x} + 4\sqrt{7x}$$

$$-2\sqrt{7x}$$

$$3\sqrt{7mn} + \sqrt{7mn} - 5\sqrt{7mn}$$

$$-\sqrt{7mn}$$

### Add and Subtract Square Roots that Need Simplification

Simplify

$$\sqrt{20} = \sqrt{4} \cdot \sqrt{5}$$

$$2\sqrt{5}$$

$$\sqrt{20} + 3\sqrt{5}$$

$$2\sqrt{5} + 3\sqrt{5}$$

$$5\sqrt{5}$$

$$\sqrt{18} + 6\sqrt{2}$$

$$3\sqrt{2} + 6\sqrt{2}$$

$$9\sqrt{2}$$

$$\sqrt{48} - \sqrt{75}$$

$$4\sqrt{3} - 5\sqrt{3}$$

$$\sqrt{32} - \sqrt{18}$$

$$4\sqrt{2} - 3\sqrt{2}$$

$$\sqrt{20} - \sqrt{45}$$

$$2\sqrt{5} - 3\sqrt{5}$$

$$-\sqrt{3}$$

$$\sqrt{2}$$

$$-\sqrt{5}$$

26.52

$$5\sqrt{18}$$

$$\sqrt{18} = 3\sqrt{2}$$

$$5(3\sqrt{2})$$

$$15\sqrt{2}$$

$$\frac{3}{4} \cdot \frac{8}{1} = \frac{24}{4} = 6$$

$$\frac{24}{15}\sqrt{2} - \frac{10}{15}\sqrt{2}$$

$$\frac{14}{15}\sqrt{2}$$

$$\sqrt{9} \cdot \sqrt{2}$$

$$3\sqrt{2}$$

$$5\sqrt{18} - 2\sqrt{8}$$

$$15\sqrt{2} - 4\sqrt{2}$$

$$11\sqrt{2}$$

$$4\sqrt{27} - 3\sqrt{12}$$

$$4(3\sqrt{3}) - 3(2\sqrt{3})$$

$$12\sqrt{3} - 6\sqrt{3}$$

$$6\sqrt{3}$$

$$3\sqrt{20} - 7\sqrt{45}$$

$$3(2\sqrt{5}) - 7(3\sqrt{5})$$

$$6\sqrt{5} - 21\sqrt{5}$$

$$-15\sqrt{5}$$

$$\frac{3}{4}\sqrt{192} - \frac{5}{6}\sqrt{108}$$

$$\frac{3}{4}(8\sqrt{3}) - \frac{5}{6}(6\sqrt{3})$$

$$6\sqrt{3} - 5\sqrt{3}$$

$$\sqrt{3}$$

$$\frac{2}{5}\sqrt{32} - \frac{1}{3}\sqrt{8}$$

$$\frac{2}{5}(4\sqrt{2}) - \frac{1}{3}(2\sqrt{2})$$

$$\frac{8}{5}\sqrt{2} - \frac{2}{3}\sqrt{2}$$

$$\sqrt{32m^7} - \sqrt{50m^7}$$

$$4m^3\sqrt{2m} - 5m^3\sqrt{2m}$$

$$-m^3\sqrt{2m}$$

$$\frac{2}{3}\sqrt{108} - \frac{5}{7}\sqrt{147}$$

$$\frac{2}{3}(6\sqrt{3}) - \frac{5}{7}(7\sqrt{3})$$

$$4\sqrt{3} - 5\sqrt{3}$$

$$-\sqrt{3}$$

$$\frac{1}{3}\sqrt{80} - \frac{1}{4}\sqrt{125}$$

$$\frac{1}{3}(4\sqrt{5}) - \frac{1}{4}(5\sqrt{5})$$

$$\frac{4}{3}\sqrt{5} - \frac{5}{4}\sqrt{5}$$

$$\frac{16}{12}\sqrt{5} - \frac{15}{12}\sqrt{5}$$

$$\frac{1}{12}\sqrt{5}$$

$$\frac{\sqrt{5}}{12}$$

$$4 \cdot 12$$

$$2\sqrt{12}$$

$$3\sqrt{18x^2} - 6x\sqrt{32} + 2\sqrt{50x^2}$$

$$3(3x\sqrt{2}) - 6x(4\sqrt{2}) + 2(5x\sqrt{2})$$

$$9x\sqrt{2} - 24x\sqrt{2} + 10x\sqrt{2}$$

$$-5x\sqrt{2}$$

$$4\sqrt{24x^2} - \sqrt{54x^2} + \frac{1}{2}x\sqrt{36}$$

$$4(2x\sqrt{6}) - 3x\sqrt{6} + 3x$$

$$8x\sqrt{6} - 3x\sqrt{6} + 3x$$

$$5x\sqrt{6} + 3x$$

$$\begin{aligned}x + x^2 \\ x \cdot x^2 = x^3\end{aligned}$$

What you will learn about:  
Multiplying Square Roots

$$\sqrt{a} \cdot \sqrt{b} = \sqrt{ab}$$

Simplify:

$$\sqrt{2} \cdot \sqrt{6}$$

$$\begin{matrix}\sqrt{12} \\ 2\sqrt{3}\end{matrix}$$

$$(6\sqrt{2})(3\sqrt{10})$$

$$\begin{matrix}18\sqrt{20} \\ 18(2\sqrt{5}) \\ 36\sqrt{5}\end{matrix}$$

$$\frac{4}{108}$$

$$(4\sqrt{3})(2\sqrt{12})$$

$$\begin{matrix}8\sqrt{36} \\ 8 \cdot 6 \\ 48\end{matrix}$$

$$(\sqrt{6x^3})(\sqrt{3x})$$

$$\begin{matrix}\sqrt{18x^4} \\ 3x^2\sqrt{2}\end{matrix}$$

$$(6\sqrt{3})(5\sqrt{6})$$

$$\begin{matrix}30\sqrt{18} \\ 30(3\sqrt{2}) \\ 90\sqrt{2}\end{matrix}$$

$$(\sqrt{2y^2})(\sqrt{50y^3})$$

$$\begin{matrix}\sqrt{100y^5} \\ 10y^2\sqrt{y}\end{matrix}$$

$$\frac{24}{144}$$

$$(10\sqrt{6p^3})(3\sqrt{18p^2})$$

$$\begin{matrix}30\sqrt{108p^5} \\ 30(6p^2\sqrt{3p}) \\ 180p^2\sqrt{3p}\end{matrix}$$

$$(2\sqrt{6y^3})(12\sqrt{30y^3})$$

$$\begin{matrix}24\sqrt{180y^6} \\ 24(6y^3\sqrt{5}) \\ 144y^3\sqrt{5}\end{matrix}$$

$$(\sqrt{2})^2 = \sqrt{4}$$

$$= 2$$

$$(-\sqrt{11})^2$$

$$11$$

$$(-\sqrt{20})^2$$

$$20$$

$$(6\sqrt{11})(5\sqrt{11})$$

$$30(11)$$

$$330$$

$$(5\sqrt{8})^2$$

$$25 \cdot 8$$

$$200$$

$$(-4\sqrt{6})^2$$

$$(16)(16)$$

$$96$$

Squaring a Square Root  
If  $a$  is a nonnegative real number, then

$$(\sqrt{a})^2 = a$$

Using Polynomial Multiplication  
to Multiply Square Roots

$$3(5 - \sqrt{2})$$

$$15 - 3\sqrt{2}$$

$$\sqrt{2}(4 - \sqrt{10})$$

$$4\sqrt{2} - \sqrt{20}$$

$$4\sqrt{2} - 2\sqrt{5}$$

$$\sqrt{7}(1 + \sqrt{14})$$

$$\sqrt{7} + \sqrt{98}$$

$$\sqrt{7} + 7\sqrt{2}$$

$$\sqrt{5}(7 + 2\sqrt{5})$$

$$7\sqrt{5} + 2\sqrt{25}$$

$$7\sqrt{5} + 10$$

$$\sqrt{6}(\sqrt{2} + \sqrt{18})$$

$$\sqrt{12} + \sqrt{108}$$

$$2\sqrt{3} + 6\sqrt{3}$$

$$8\sqrt{3}$$

$$\sqrt{12}(\sqrt{3} + \sqrt{24})$$

$$\sqrt{36} + \sqrt{288}$$

$$6 + 12\sqrt{2}$$

$$\begin{array}{r} 24 \\ 12 \\ \hline 240 \end{array}$$

$$(2 + \sqrt{3})(4 - \sqrt{3})$$

$$8 - 2\sqrt{3} + 4\sqrt{3} - 3$$

$$5 + 2\sqrt{3}$$

$$(4 - \sqrt{10})(2 + \sqrt{10})$$

$$8 + 4\sqrt{10} - 2\sqrt{10} - 10$$

$$-2 + 2\sqrt{10}$$

$$(3\sqrt{2} - \sqrt{5})(\sqrt{2} + 4\sqrt{5})$$

$$6 + 12\sqrt{10} - \sqrt{10} - 20$$

$$-14 + 11\sqrt{10}$$

$$(\sqrt{6} - 3\sqrt{8})(2\sqrt{6} - \sqrt{8})$$

$$12 - \sqrt{48} - 6\sqrt{48} + 24$$

$$36 - 7\sqrt{48}$$

$$36 - 28\sqrt{3}$$

$$\begin{array}{r} \downarrow \\ \sqrt{48} = \sqrt{16 \cdot 3} \\ 4\sqrt{3} \end{array}$$

$$(10 + \sqrt{2})^2$$

$$(10 + \sqrt{2})(10 + \sqrt{2})$$

$$100 + 20\sqrt{2} + 2$$

$$102 + 20\sqrt{2}$$

$$(4 - 2\sqrt{5})^2$$

$$16 - 16\sqrt{5} + 20$$

$$36 - 16\sqrt{5}$$

$$(3 - 4\sqrt{n})^2$$

$$9 - 24\sqrt{n} + 16n$$

Conjugates

$$(4 + \sqrt{2})(4 - \sqrt{2})$$

$$16 - 4\sqrt{2} + 4\sqrt{2} - 2$$

$$14$$

$$(5 - 2\sqrt{3})(5 + 2\sqrt{3})$$

$$25 + 10\sqrt{3} - 10\sqrt{3} - 12$$

$$13$$

$$(4 + 5\sqrt{7})(4 - 5\sqrt{7})$$

$$(3 - 2\sqrt{5})(3 + 2\sqrt{5})$$