

What you will learn about:  
Graphs of Linear Inequalities

**LINEAR INEQUALITY**

A linear inequality is an inequality that can be written in one of the following forms:

$$Ax + By > C \quad Ax + By \geq C \quad Ax + By < C \quad Ax + By \leq C$$

where  $A$  and  $B$  are not both zero.

Determine whether each ordered pair is a solution to the inequality  $y > x + 4$

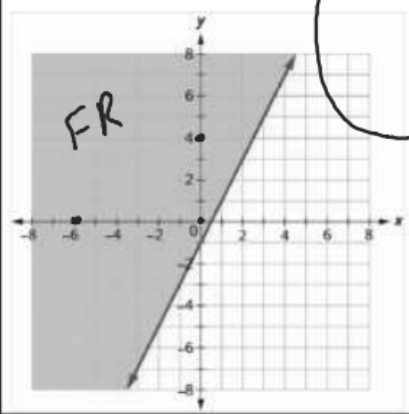
$<, >$   
open dot  
Dotted line

$\leq, \geq$   
closed dot  
Solid line

|             |              |              |              |               |
|-------------|--------------|--------------|--------------|---------------|
| a) (0, 0)   | b) (1, 6)    | c) (2, 6)    | d) (5, 15)   | e) (-8, 12)   |
| $0 > 0 + 4$ | $6 > 1 + 4$  | $6 > 2 + 4$  | $15 > 5 + 4$ | $12 > -8 + 4$ |
| $0 > 4$     | $6 > 4$      | $6 > 6$      | $15 > 9$     | $12 > -4$     |
| No Solution | Yes Solution | Not Solution | Yes Solution | Yes Solution  |

|  |  |
|--|--|
| $Ax + By < C$                              | $Ax + By \leq C$                       |
| $Ax + By > C$                              | $Ax + By \geq C$                       |
| Boundary line is not included in solution. | Boundary line is included in solution. |
| Boundary line is dashed.                   | Boundary line is solid.                |

The boundary line shown is  $y = 2x - 1$ . Write the inequality shown by the graph.



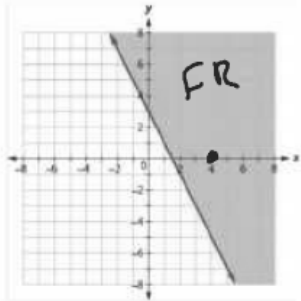
$\leq$  or  $\geq$

$0 \geq 2(0) - 1$

$0 \geq -1$

$y \geq 2x - 1$

The boundary line shown is  $y = -2x + 3$ . Write the inequality shown by the graph.



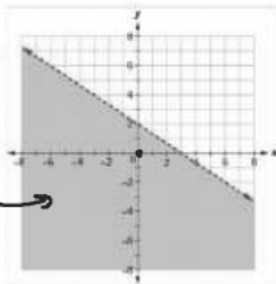
$$\leq, \geq \quad (4, 0)$$

$$0 \geq -2(4) + 3$$

$$0 \geq -5$$

$$y \geq -2x + 3$$

The boundary line shown is  $2x + 3y = 6$ . Write the inequality shown by the graph.



$$<, >$$

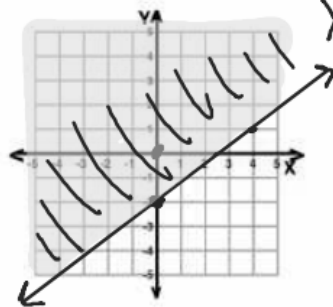
$$2(0) + 3(6) \quad 6$$

$$0 < 6$$

$$2x + 3y < 6$$

Linear Inequality  
Feasible Region

Graph the linear inequality  $y \geq \frac{3}{4}x - 2$ .

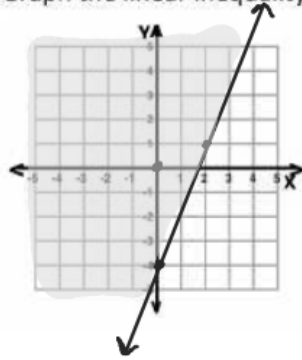


$$y = \frac{3}{4}x - 2$$

$$0 \geq \frac{3}{4}(0) - 2$$

$$0 \geq -2 \quad \checkmark$$

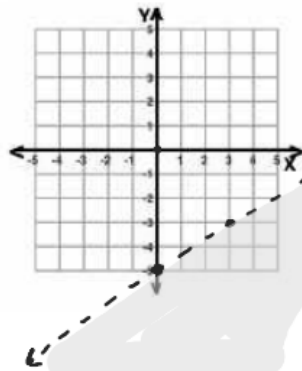
Graph the linear inequality  $y \geq \frac{5}{2}x - 4$ .



$$0 \geq \frac{5}{2}(0) - 4$$

$$0 \geq -4 \quad \checkmark$$

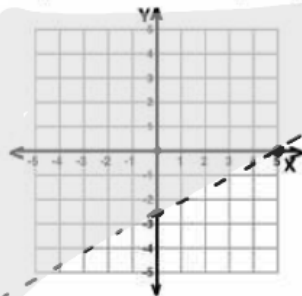
Graph the linear inequality  $y < \frac{2}{3}x - 5$ .



$$0 < \frac{2}{3}(0) - 5$$

$$0 < -5$$

Graph the linear inequality  $x - 2y < 5$ .



$$x - \frac{c}{A} = \frac{5}{1} = 5 \quad (5, 0)$$

$$y = \frac{c}{B} = \frac{5}{-2} = \left(0, -\frac{5}{2}\right)$$

$$0 - 2(0) < 5$$

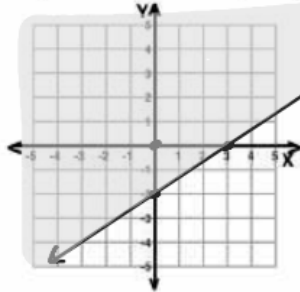
$$0 < 5$$

$$x - 2y < 5$$

$$-2y < -x + 5$$

$$y > \frac{1}{2}x - \frac{5}{2}$$

Graph the linear inequality  $2x - 3y \leq 6$ .



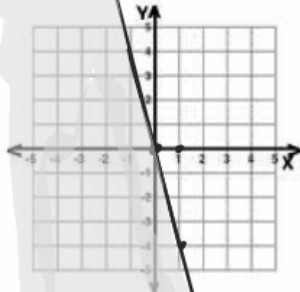
$$x = \frac{c}{A} = \frac{6}{2} = (3, 0)$$

$$y = \frac{c}{B} = \frac{6}{-3} = (0, -2)$$

$$2(0) - 3(0) \leq 6$$

$$0 \leq 6$$

Graph the linear inequality  $y \leq -4x$ .



$$b = 0$$

$$m = \frac{-4}{1}$$

$$(1, 0)$$

$$0 \leq -4(1)$$

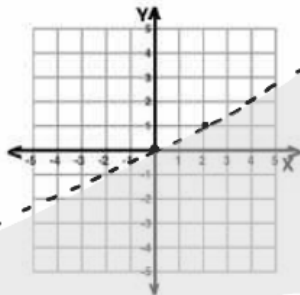
$$0 \leq -4x$$

$$(1, 0)$$

$$2(1) - 4(0) > 0$$

$$2 > 0$$

Graph the linear inequality  $2x - 4y > 0$



$$x = \frac{0}{2} = (0, 0)$$

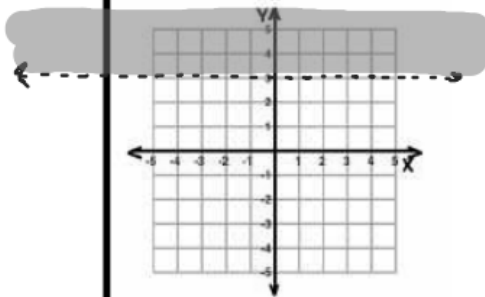
$$y = \frac{0}{4} = (0, 0)$$

$$m = -\frac{A}{B}$$

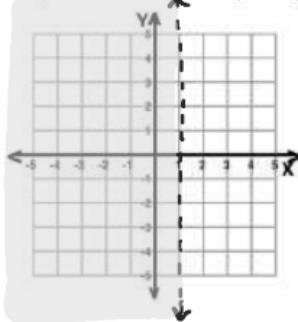
$$= -\frac{2}{-4} = \frac{1}{2}$$

Graph the linear inequality  $y > 3$ .

$$y = 3$$

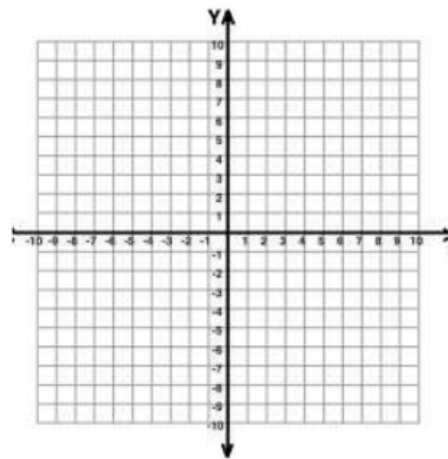


Graph the linear inequality  $x < 1$ .



Find the feasible region.

$$\begin{aligned}x &\geq 1 \\y &\leq 6 \\y &\geq x - 2\end{aligned}$$



Find the feasible region.

$$\begin{aligned}2x + y &\geq 4 \\x - y &< -1\end{aligned}$$

