

What you will learn about:  
Solving Inequalities

$$x = 10$$

$$x + 5 = 15$$

$$x + 5 > 15$$

$\leq, \geq$  solid dot

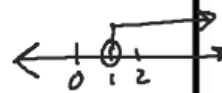
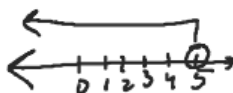
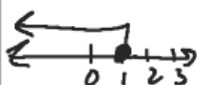
$<, >$  open dot

Graph on a number line

$$x \leq 1$$

$$x < 5$$

$$x > 1$$



Interval Notation

$\leq, \geq$  [ ]

$<, >$  ( )

Smaller #, Larger #

$$\begin{array}{r} 3q \\ -23 \\ \hline 19 \end{array}$$

$$18 \geq 42 - 23$$

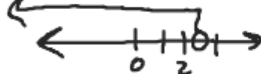
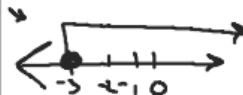
$$18 \geq 19$$

Graph on the number line and write in interval notation

$$x \geq -3$$

$$x < 2.5$$

$$x \leq -\frac{3}{5}$$



$$[-3, \infty)$$

$$(-\infty, 2.5)$$

$$(-\infty, -\frac{3}{5}]$$

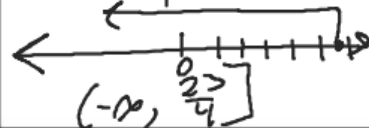
Solve each inequality, graph the solution on the number line, and write the solution in interval notation.

$$3q \geq 7q - 23$$

$$\begin{array}{r} -7q \quad -7q \\ \hline \end{array}$$

$$\begin{array}{r} -4q \geq -23 \\ -4 \quad -4 \\ \hline \end{array}$$

$$q \leq \frac{23}{4}$$

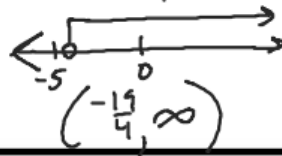


$$6x < 10x + 19$$

$$\begin{array}{r} -10x \quad -10x \\ \hline \end{array}$$

$$\begin{array}{r} -4x < 19 \\ -4 \quad -4 \\ \hline \end{array}$$

$$x > -\frac{19}{4}$$



$$-24 < -40q$$

$$-24 < -21$$

Solve each inequality, graph the solution on the number line, and write the solution in interval notation.

$$24 - 27 > 21 - 28$$

$$-3 > -7$$

$$8p + 3(p - 12) > 7p - 28$$

$$8p + 3p - 36 > 7p - 28$$

$$11p - 36 > 7p - 28$$

$$-7p \quad -7p$$

$$4p - 36 > -28$$

$$4p > 8$$

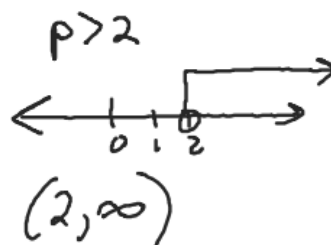
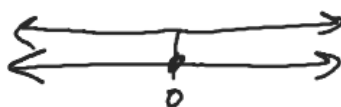
$$8x - 2(5 - x) < 4(x + 9) + 6x$$

$$8x - 10 + 2x < 4x + 36 + 6x$$

$$10x - 10 < 10x + 36$$

$$-10 < 36$$

$$(-\infty, \infty)$$

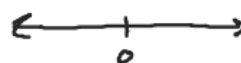


$$24 \left( \frac{1}{3}a \right) - \left( \frac{1}{8}a \right) > \left( \frac{5}{24}a \right) + \left( \frac{3}{4} \right) 24$$

$$8a - 3a > 5a + 18$$

$$5a > 5a + 18$$

$$0 > 18$$



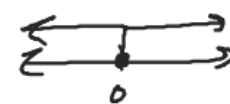
$$(\emptyset)$$

$$24 \left( \frac{1}{4}x \right) - \left( \frac{1}{12}x \right) \leq \left( \frac{1}{6}x \right) + \left( \frac{7}{8} \right) 24$$

$$6x - 2x \leq 4x + 21$$

$$4x \leq 4x + 21$$

$$0 \leq 21$$



$$(-\infty, \infty)$$

$>$	$\geq$	$<$	$\leq$
is greater than	is greater than or equal to	is less than	is less than or equal to
is more than	is at least	is smaller than	is at most
is larger than	is no less than	has fewer than	is no more than
exceeds	is the minimum	is lower than	is the maximum

Translate and solve. Then write the solution in interval notation and graph on the number line.

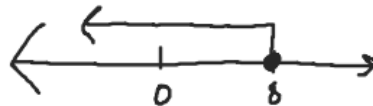
$$\begin{array}{r} 8 \\ 12 \overline{)96} \\ \underline{96} \\ 0 \end{array}$$

Twelve times a number is no more than 96.

$$12x \leq 96$$

$$x \leq 8$$

$$(-\infty, 8]$$

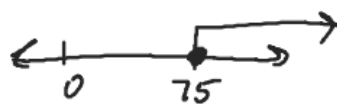


Thirty less than  $x$  is at least 45.

$$x - 30 \geq 45$$

$$x \geq 75$$

$$[75, \infty)$$

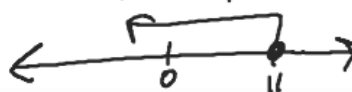


Four more than a number is at most 15.

$$x + 4 \leq 15$$

$$x \leq 11$$

$$(-\infty, 11]$$



$$\frac{1}{6}(1 - 6x) = -\frac{1}{3}\left(6x + \frac{1}{2}\right)$$

$$46. \quad \frac{1}{2}\left(2t - \frac{3}{4}\right) + \frac{2}{5} = \frac{4}{5}t$$

$$\frac{3}{8}(m + 8) - \frac{3}{16} = 2\left(m + \frac{3}{4}\right) + \frac{1}{2}$$

$$48. \quad 0.3(x + 5) = 5(0.1 + 0.11x)$$

$$3.75 - 2.5(p + 1) = 0.5p + 4.25$$

$$50. \quad 2.3y = 0.15(2y - 3) - 0.6$$

$\frac{3}{8}\left(\frac{3}{4}\right)$   
24

**Work Outside the Box:**

*Write each.*

$$\frac{2x - 18}{4} = \frac{3x + 1}{2}$$

$$52. \quad \frac{x + 9}{5} = \frac{x - 7}{10}$$

$$\frac{x + 3}{8} - \frac{x}{2} = 5$$

$$54. \quad \frac{x - 5}{6} = \frac{x}{4} - 1$$

$$\frac{3}{8}(m+8) - \frac{3}{16} = 2\left(m + \frac{3}{4}\right) + \frac{1}{2}$$

$$3.75 - 2.5(p+1) = 0.5p + 4.25$$

$$3.75 - 2.5p - 2.5 = .5p + 4.25$$

**nk Outside the Box:**

$$1.25 - 2.5p = .5p + 4.25$$

re each.

$$\begin{aligned} -3p &= 3 \\ p &= -1 \end{aligned}$$

$$\frac{2x-18}{4} \overset{\curvearrowright}{\curvearrowleft} \frac{3x+1}{2}$$

$$2(2x-18) = 4(3x+1)$$

$$4x - 36 = 12x + 4$$

$$-36 = 8x + 4$$

$$-40 = 8x$$

$$x = -5$$

$$\left(\frac{x+3}{8}\right) - \left(\frac{x}{2}\right)^8 = (5)^8$$

$$x+3 - 4x = 40$$

$$-3x + 3 = 40$$

$$-3x = 37$$

$$x = -\frac{37}{3}$$

$$6(m+8) - 3 = 32\left(m + \frac{3}{4}\right) + 8$$

$$6m + 48 - 3 = 32m + 24 + 8$$

$$6m + 45 = 32m + 32$$

$$13 = 26m$$

$$m = \frac{1}{2}$$