

Simplify

$$12 - 3(9 - 12)$$

$$12 - 3(-3)$$

$$12 - (-9)$$

$$21$$

$$12(-9) \div (-3)^3$$

$$-108 \div (-27)$$

$$4$$

$$16 - 6(7 - 13)$$

$$16 - 6(-6)$$

$$16 + 36$$

$$52$$

$$-30 \div 2 + (-3)(-7)$$

$$-15 + 21$$

$$6$$

Evaluate the following when $x = -5$

$$2x^2 + 3x + 8$$

$$2(-5)^2 + 3(-5) + 8$$

$$2(25) + (-15) + 8$$

$$50 + (-15) + 8$$

$$43$$

$$-3x^2 - 2x + 6$$

$$-3(-5)^2 - 2(-5) + 6$$

$$-3(25) - (-10) + 6$$

$$-75 + 10 + 6$$

$$-59$$

Translate Phrases to Expression
with integers

Translate and simplify the sum of eight and negative twelve,
increased by three

$$(8 + (-12)) + 3$$

$$-4 + 3 = -1$$

Translate and simplify the difference of negative eight and negative
twelve, increased by nine.

$$(-8 - (-12)) + 9$$

$$4 + 9$$

$$13$$

The temperatures in Urbana, Illinois one morning was 11 degrees. By mid-afternoon, the temperature had dropped to -9 degrees. What was the different of the morning and afternoon temperatures?

$$11 - (-9) = 20$$

The Mustanges football team received three penalties in the third quarter. Each penalty gave them a loss of fifteen yards. What was the number of yards lost?

$$3(-15) = -45 \text{ yds}$$

Bill uses the ATM on campus because ^{it} is convenient. However, each time he uses it he is charged a \$2 fee. Last month he used the ATM eight times. How much was his total fee for using the ATM?

$$-2(8) = -16$$

At the first down, the Chargers had the ball on their 25 yard line. On the next three downs, they lost 6 yards, gained 10 yards, and lost eight yards. What was the yard line at the end of the fourth down?

$$25 - 6 = 19 + 10 = 29 - 8 = \underline{21 \text{ yd line}}$$

Mayra has \$124 in her checking account. She writes a check for \$152. What is her new balance in her checking account.

$$124 - 152 = -28$$

What you will learn about:
Visualize Fractions

Equivalent Fractions

Property of one

Any number divided
by itself is 1

Equivalent Fractions

Fractions that
have the same value

Equivalent Fractions Property

$$\frac{a}{b} = \frac{a \cdot c}{b \cdot c}$$

Simplified Fraction

If there are no
common factors other
than 1 in numerator
and denominator

Fraction $\frac{a}{b}$, where $b \neq 0$.

- a is the numerator and b is the denominator

Find three fractions equivalent to $\frac{2}{5}$.

$$\frac{4}{10}, \frac{6}{15}, \frac{20}{50}$$

Find three fractions equivalent to $\frac{5}{8}$.

$$\frac{10}{16}, \frac{50}{80}, \frac{500}{800}$$

Simplify: $-\frac{32}{56} = -\frac{4}{7}$

Simplify:

$$-\frac{42}{54} - \frac{7}{9}$$

$$\frac{45}{81} = \frac{5}{9}$$

$$\frac{36}{48} = \frac{6}{8} = \frac{3}{4}$$

Using Prime Numbers to Simplify Fractions

Simplify

$$\frac{210}{385}$$

$$-\frac{2 \cdot 3 \cdot 5 \cdot 7}{5 \cdot 7 \cdot 11}$$

$$-\frac{6}{11}$$

$$\frac{3x}{3y} = \frac{x}{y}$$

$$\frac{69}{120}$$

$$-\frac{3 \cdot 23}{2 \cdot 2 \cdot 2 \cdot 3 \cdot 5}$$

$$\frac{23}{40}$$

$$\frac{x}{xy} = \frac{1}{y}$$

$$-\frac{120}{192}$$

$$-\frac{2 \cdot 2 \cdot 2 \cdot 2 \cdot 3}{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2 \cdot 3}$$

$$-\frac{5}{8}$$

$$\frac{192}{24}$$

$$\frac{2 \cdot 96}{2 \cdot 48}$$

$$\frac{2 \cdot 48}{2 \cdot 24}$$

$$\frac{24}{12}$$

$$\frac{12}{6}$$

$$\frac{6}{3}$$

$$\frac{2}{1}$$

Fraction Multiplication

$$\begin{array}{r} 4 \\ 28 \\ \underline{15} \\ 140 \\ \underline{280} \\ 420 \\ 48 \\ \underline{5) 240} \\ 20 \\ \underline{20} \\ 40 \end{array}$$

$$-\frac{11}{12} \cdot \frac{5}{7} = -\frac{55}{84}$$

$$-\frac{20}{7} \cdot \frac{8}{15} = -\frac{80}{105}$$

$$-\frac{16}{21}$$

$$-\frac{8}{42}$$

$$-\frac{4}{21}$$

$$\frac{3}{4} \cdot \frac{1}{4} = \frac{3}{16}$$

$$\frac{45}{240} = \frac{3 \cdot 3 \cdot 5}{2 \cdot 2 \cdot 2 \cdot 2 \cdot 3 \cdot 5}$$

$$\frac{3}{16}$$

$$-\frac{12}{5}(-20x)$$

$$\left(-\frac{12}{5}\right)\left(-\frac{20x}{1}\right)$$

$$48x$$

$$\frac{11}{3}(-9a)$$

$$\left(\frac{11}{3}\right)\left(-\frac{9a}{1}\right) = -\frac{99a}{3}$$

$$-33a$$

$$\frac{240}{8} = 30$$

$$\frac{24}{3} = 8$$

$$\frac{10}{5} = 2$$

Dividing Fractions

Reciprocal

Flip the fraction

Copy Dot Flip

Keep Change Change

Mult by reciprocal

Divide:

$$-\frac{2}{3} \div \frac{n}{5}$$

$$-\frac{2}{3} \cdot \frac{5}{n}$$

$$-\frac{10}{3n}$$

$$-\frac{7}{8} \div \left(-\frac{14}{27}\right)$$

$$-\frac{7}{8} \cdot -\frac{27}{14}$$

$$\frac{27}{16}$$

$$-\frac{7}{27} \div \left(-\frac{35}{36}\right)$$

$$-\frac{7}{27} \cdot \left(-\frac{36}{35}\right)$$

$$\frac{4}{15}$$

Complex Fraction

Simplify

$$\frac{\frac{3}{4}}{\frac{5}{8}} = \frac{3}{4} \div \frac{5}{8} = \frac{3}{4} \cdot \frac{8}{5} = \frac{6}{5}$$

$$\frac{\frac{12}{15}}{\frac{6}{1}} = \frac{12}{15} \div \frac{6}{1} = \frac{12}{15} \cdot \frac{1}{6} = \frac{12}{90} = \frac{2}{15}$$

$$\frac{\frac{x}{2}}{\frac{xy}{6}} = \frac{x}{2} \div \frac{xy}{6} = \frac{x}{2} \cdot \frac{6}{xy} = \frac{6x}{2xy} = \frac{3}{y}$$

Simplify

$$\frac{4-2(3)}{2^2+2} = \frac{4-6}{4+2} = \frac{-2}{6} = -\frac{1}{3}$$

$$\frac{3^3-2(-4)}{4^2+4} = \frac{27-(-8)}{16+4} = \frac{35}{20} = \frac{7}{4}$$

Placement of Negative Sign in a Fraction

$$-\frac{a}{b}$$

$$\frac{a}{-b}$$

$$-\frac{a}{b}$$

Simplify:

$$\frac{4(-3)+6(-2)}{-3(2)-2} = \frac{-24}{-8} = 3$$

$$\frac{8(-2)+4(-3)}{-5(2)+3} = \frac{-16+-12}{-7} = \frac{-28}{-7} = 4$$

Translate Phrase to Expressions with Fractions

Translate the English phrase into an algebraic expression: the quotient of the difference of m and n, and p.

Translate the English phrase into an algebraic expression: the quotient of the difference of a and b, and cd.

Translate the English phrase into an algebraic expression: the quotient of A and the difference 3 and B.

A recipe for chocolate chip cookies calls for $\frac{3}{4}$ cup brown sugar. Imelda wants to double the recipe. How much brown sugar will Imelda need? Show your calculation.

Nina is making 4 pans of fudge to serve after a music recital. For each pan, she needs $\frac{2}{3}$ cup of condensed milk. How much condensed milk will Nina need? Show your calculation.

Measuring cups usually come in sets of $\frac{1}{4}$, $\frac{1}{3}$, $\frac{1}{2}$, and 1 cup. Draw a diagram to show two different ways that Nina could measure the condensed milk needed for 4 pans of fudge.

Kristen has $\frac{3}{4}$ yards of ribbon that she wants to cut into 6 equal parts to make hair ribbons for her daughter's dolls. How long will each ribbon be?

Rafael wanted to order half a medium pizza at a restaurant. The waiter told him that a medium pizza could be cut into 6 or 8 slices. Would he prefer 3 out of 6 slices or 4 out of eight slices? Rafael replied that since he wasn't very hungry, he would prefer 3 out of 6 slices. Explain what is wrong with Rafael's reasoning.